

Solving Log Equations A11

Solve each log equation. Be sure to check your answers.

1. $\log_5 5x = 2$
 $\frac{5^2 - 5x}{5} = 5$
 $x = 5$
2. $\log_2(2x - 3) = 2$
 $2^2 = 2x - 3$
 $4 = 2x - 3$
 $7 = 2x$
 $x = \frac{7}{2}$
3. $2 \log_4 x = 3$
 $4^3 = x^2$
 $x = 8$
4. $\ln(x + 3) = 4$
 $e^4 = x + 3$
 $x = e^4 - 3$
5. $\log_{25} x = \frac{3}{2}$
 $25^{\frac{3}{2}} = x$
 $125 = x$
6. $\ln(2x) = 6$
 $e^6 = 2x$
 $x = \frac{1}{2}e^6$
7. $\log_4 5x = \log_4 2$
 $5x = 2$
 $x = \frac{2}{5}$
8. $\ln 4 - \ln x = \ln 3$
 $\ln \frac{4}{x} = \ln 3$
 $\frac{4}{x} = 3$
 $x = \frac{4}{3}$
9. $\log_3 x = 2 \log_3 3 + \log_3 5$
 $\log_3 x = \log_3 9 + \log_3 5$
 $x = 45$
10. $\log_4(3x - 1) = \log_4(2x + 3)$
 $3x - 1 = 2x + 3$
 $x = 4$
11. $\log_4(4x + 3) = \log_4(3x - 6)$
 $4x + 3 = 3x - 6$
 $x = -9$
12. $\log_5 2 + \log_5(3x - 2) = 1$
 $\log_5 6x - 4 = 1$
 $5^1 = 6x - 4$
 $9 = 6x$
 $x = \frac{3}{2}$
13. $2 \log_3 6 + \frac{1}{2} \log_3 16 = \log_3 x$
 $\log_3 36 + \log_3 2 = \log_3 x$
 $x = 72$
14. $\log_8(x^2 + 16) = \log_8 80$
 $x^2 + 16 = 80$
 $x^2 = 64$
 $x = 8$
 $x = -8$
15. $\log_5(x^2 + 7) = \frac{2}{3} \log_5(64)$
 $x^2 + 7 = 16$
 $x^2 = 9$
 $x = 3$
 $x = -3$

Exponential and Logarithmic Equations

Part 1: Find the solution of the exponential equation, correct to four decimal places.

1. $6^x = 12$
2. $10^{-x} = 2$
3. $3^{2x-4} = 5$
4. $2e^{3x} = 17$
5. $e^{-(1+10^x)} = 9$
6. $2^{2^x} = 34$
7. $3^{\frac{1}{x}} = 0.1$
8. $e^{2-4x} = 16$
9. $\left(\frac{1}{4}\right)^x = 75$
10. $10^{2x} = e^4$
11. $7^{\frac{1}{x}} = 5^{1-x}$
12. $3^{2x+4} = e^{x+3}$
13. $\frac{10}{1+x^2} = 2$
14. $(1.00025)^{12x} = 2$
15. $6(2)^{2x-1} - 1 = 4$
16. $\ln(x+2) = \ln(4x+5)$
17. $\log_2(x+1) = \log_2 20$
18. $2 \log_3 x = \log_3 2 + \log_3(3x-4)$
19. $\log_2 3 + \log_2 x = \log_2 5 + \log_2(x-2)$
20. $\log_2(x-1) - \log_2(x+6) = \log_2(x-2) - \log_2(x+3)$
21. $\log_4(x-1) - \log_4(x-1) - \log_4(2x+1)$
22. $\log_2(x+2) = 4$
22. $\log_2(x+1) - 2 = \log_2(x-1)$
23. $\log_2(x+1) - 2 = \log_2(x-1)$
24. $\ln(3x+4) = 3$
24. $2 \log_2 x - \log_2 9 = 2$
25. $2 \log_2 x - \log_2 9 = 2$
26. $\log_2(3x-2) - \log_2 x = 3$
27. $\log_2(x+2) = 2$
28. $\log_2 \frac{1}{x} + 2 \log_2 x = 3$
29. $\log_2(x-1) + \log_2(x+2) = 1$
30. $\log_2(x^2 - x - 2) = 2$

Part 2: Solve the logarithmic equation for x.

16. $\ln(x+2) = \ln(4x+5)$
17. $\log_2(x+1) = \log_2 20$
18. $2 \log_3 x = \log_3 2 + \log_3(3x-4)$
19. $\log_2 3 + \log_2 x = \log_2 5 + \log_2(x-2)$
20. $\log_2(x-1) - \log_2(x+6) = \log_2(x-2) - \log_2(x+3)$
21. $\log_4(x-1) - \log_4(x-1) - \log_4(2x+1)$
22. $\log_2(x+2) = 4$
22. $\log_2(x+1) - 2 = \log_2(x-1)$
23. $\log_2(x+1) - 2 = \log_2(x-1)$
24. $\ln(3x+4) = 3$
24. $2 \log_2 x - \log_2 9 = 2$
25. $2 \log_2 x - \log_2 9 = 2$
26. $\log_2(3x-2) - \log_2 x = 3$
27. $\log_2(x+2) = 2$
28. $\log_2 \frac{1}{x} + 2 \log_2 x = 3$
29. $\log_2(x-1) + \log_2(x+2) = 1$
30. $\log_2(x^2 - x - 2) = 2$